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Abstract

Pre-resonant Raman effect of chromate ion, CrO_4^{2-} , was observed in a metasilicate glass with molar composition $2Na_2O \cdot 1CaO \cdot 3SiO_2$ containing 1.0 wt% of Cr_2O_3 . Raman spectra were measured by the conventional 90° scattering geometry and by the microprobe Raman spectroscopic techniques. The presence of chromate ions in the glass is favoured by the glass composition and oxidizing conditions during the glass melting, and they are responsible for optical absorption bands at 370 and 250 nm. Raman spectrum of the undoped glass presents bands at 625, 860 and 980 cm⁻¹, and the presence of chromate ions gives rise to additional bands at 365, 850 and a shoulder at 890 cm⁻¹. An enhancement of the 850 cm⁻¹ Raman band is observed with decreasing laser exciting wavelength. The exciting frequency dependence of the intensity of this band is discussed in terms of theoretical models given in the literature.

1. Introduction

The resonant Raman effect consists of an anomalous increase in the intensity of the scattered radiation, as the exciting radiation frequency equals the absorption frequency of a molecule [1]. The pre-resonant Raman effect occurs when the virtual state in the Raman transition coincides with lower energy levels of allowed electronic transitions in the molecule, and the scattered radiation has a lower intensity than in the resonant case [1]. The anomalous increase of the scattered radiation intensity, I_s , with the exciting frequency, $\tilde{\nu}_i = \lambda_i^{-1}$, is due to the dependence of the Raman scattering tensor with this frequency. This dependence causes a deviation of the fourth power law, $I_s \propto \tilde{\nu}_i^4$, for the scattered radiation intensity [1].

Based on early theories, Albrecht and Hutley [2] analyzed the experimental intensity dependence of the 1334 cm⁻¹ Raman band of *p*-nitroaniline, dissolved in benzene [3], with the exciting frequency when one or two electronic transitions are involved. They used the adimensional factors F_A^2 and F_B^2 :

$$I_{s} \propto F_{A}^{2} = \left[\frac{\tilde{\nu}_{s}^{2}(\tilde{\nu}_{e}^{2} + \tilde{\nu}_{i}^{2})}{\left(\tilde{\nu}_{e}^{2} - \tilde{\nu}_{i}^{2}\right)^{2}}\right]^{2}, \qquad (1)$$

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and

$$I_{\rm s} \propto F_{\rm B}^2 = \left[\frac{2\tilde{\nu}_{\rm s}^2 \left(\tilde{\nu}_{\rm e}\tilde{\nu}_{\rm f} + \tilde{\nu}_{\rm i}^2\right)}{\left(\tilde{\nu}_{\rm e}^2 - \tilde{\nu}_{\rm i}^2\right)\left(\tilde{\nu}_{\rm f}^2 - \tilde{\nu}_{\rm i}^2\right)}\right]^2,\tag{2}$$

where $\tilde{\nu}_{s} = \tilde{\nu}_{i} - \tilde{\nu}_{m}$ ($\tilde{\nu}_{m}$ is the frequency of the Raman band which undergoes the anomalous increase of intensity), and $\tilde{\nu}_{e}$ and $\tilde{\nu}_{f}$ are the electronic transition frequencies. Eq. (2) was found to give the best fit for pre-resonant effect in *p*-nitroaniline [2].

The resonant Raman effect was observed for many coloured solutions of organic substances [4,5]. Doing and Prendergast [6] measured the pre-resonant spectra of a solution of tryptophan and phenylalanine with ultraviolet exciting wavelength using a continuously tunable, quasi-continuous-wave laser source.

For inorganic substances, the effect is less common. Kiefer and Bernstein [7] measured the resonant Raman effect of MnO_4^{2-} ions in aqueous solutions and in KMnO₄ crystals, and of I_3^- (triiodide) ions dissolved in a solution of CHCl₂ and CS₂. The resonant effect was recently measured for uranyl nitrate dissolved in dimethyl sulfoxide [8]. The effect was also observed for molecules adsorbed on metal surfaces [9,10], superlattices [11], intrinsic germanium surfaces [12] and CdS_xSe_{1-x} semiconductor microcrystals in glasses [13].

Raman spectra of chromate ions, $\text{CrO}_4^{2^-}$, in aqueous solutions and in solid state were first measured by Venkateswaran [14], who identified the Raman bands and the corresponding vibrational modes, characteristic of tetrahedral molecules (T_d symmetry). Stammreich et al. [15] performed Raman measurements to correct the frequencies of the bands and re-evaluated the force constants for each vibrational mode of the chromate ion and the modes resulting from the interactions between the fundamental ones. Subsequent publications [16,17] confirmed these Raman frequencies and the corresponding vibrational modes, which are reported in Table 1.

Kiefer and Bernstein [18] presented pre-resonant and resonant Raman spectra of CrO_4^{2-} in solution and in K₂CrO₄ crystalline powder and confirmed the validity of Eq. (2) for the 850 cm⁻¹ Raman band which suffers change in intensity with the incident radiation frequency. They used the absorption specTable 1

Frequencies and assignments of Raman bands of chromate ions, CrO_4^{2-} , in aqueous solution, after Ref. [17]. The values in parentheses are the percentual relative intensities of the bands, and 'p' and 'dp' mean that the bands are completely polarized or depolarized, respectively

$\tilde{\nu}_{\rm m}~({\rm cm}^{-1})$	Vibrational mode	
348(27) dp	ν_2 (E): symmetric bending	
371(19) dp	ν_4 (F ₂): asymmetric bending	
846(100) p	ν_1 (A ₁): symmetric stretching	
887(21) dp	ν_3 (F ₂): asymmetric stretching	

tra obtained by Johnson and McGlynn [19]: $\tilde{\nu}_e = 26\ 900\ \text{cm}^{-1}\ (\lambda_e = 370\ \text{nm}), \ \tilde{\nu}_f = 36\ 600\ \text{cm}^{-1}\ (\lambda_f = 275\ \text{nm}).$

Raman spectra of oxide glasses containing CrO_4^{2-} were measured by Brawer and White [20] and Nelson et al. [21]. They concluded that the dissolved chromate ions are isolated in the glass matrix, since the Raman spectra of these ions, both in glasses and in aqueous solutions, are essentially the same in terms of band frequency, width and polarization. However, they made no consideration about the possibility of the observed pre-resonant Raman effect of the ion in glasses.

According to Nath and Douglas [22], during the melting in air of soda-silica glasses doped with Cr_2O_3 , the following $Cr^{3+} - Cr^{6+}$ equilibrium reaction takes place:

$$Cr_{(melt)}^{3+} + \frac{3}{2}O_{2_{(gas)}} \hookrightarrow Cr_{(melt)}^{6+} + \frac{3}{2}O_{(melt)}^{2-}.$$
 (3)

This reaction shifts to the right with the increase of alkali content in the melt.

The high concentration of modifier oxides in the $2Na_2O \cdot 1CaO \cdot 3SiO_2$ metasilicate glass and its melting in air are sufficient conditions to promote the oxidation of a considerable number of Cr^{3+} ions to Cr^{6+} ions, according to Eq. (3), in the form of CrO_4^{2-} molecular ions.

In the present work, the pre-resonant Raman effect due to $\text{CrO}_4^{2^-}$ ions in the $2\text{Na}_2\text{O} \cdot 1\text{CaO} \cdot 3\text{SiO}_2$ glass is reported, and the dependence of the intensity of the 850 cm⁻¹ Raman band with the exciting wavelength is analyzed through Eqs. (1) and (2). Raman spectra were obtained using the conventional

 90° scattering geometry and the microprobe technique.

2. Experimental

Appropriate quantities of reagent-grade sodium and calcium carbonates (Riedel deHaën, and Merck, respectively), quartz sand (Mineração Jundu) and 1.0 wt% Cr_2O_3 (Merck) were melted in a platinum crucible in a Globar furnace at 1350°C in air. The melt was homogenized during 1 h with a platinum stirrer, cast on an iron plate and pressed with a stainless steel disc. The cooling rate was higher than 400°C/min, fast enough to prevent glass crystallization. The final glass was transparent, green and without visible bubbles, striae or crystallites.

For measuring the Raman spectra at the 90° scattering geometry, the faces of a sample with dimensions about $(3 \times 4 \times 5)$ mm³ were polished to an optical degree with an aqueous slurry of cerium oxide (1.0 μ m) on a pitch tool. A sample with one partially polished surface was prepared for micro-Raman measurements.

The 90° scattering geometry Raman spectra were measured using an argon (Ar) laser (2020 Spectra Physics), a double diffraction grating spectrometer (1402 Spex) and a water cooled photomultiplier (C31034-RF Products for Research). The data were computer processed. Unpolarized spectra were measured with a resolution of about 1 cm⁻¹. The sample was positioned so that the exciting laser beam was as near as possible to the surface of the output scattered radiation. This surface was parallel to the entrance slit of the spectrometer. Such procedure was taken to minimize the absorption of the scattered radiation inside the sample.

Raman microprobe spectra of the sample surface were obtained employing a triple monochromator Micro-Raman System (XY Dilor) equipped with a multichannel detector (Gold array-detector). The sample was also excited with an Ar laser (Innova 70-2, Coherent), with output power of about 700 mW for the 514.5 and 488.0 nm laser lines and 150 mW for the 457.9 nm line.

For optical absorption spectra measurements near the ultraviolet region, a glass with the same composition and with about 0.1 wt% of Cr_2O_3 was prepared

using the same protocol. The final glass presents the same visual characteristics as the first one, except it is light yellow-greenish in colour.

Optical absorption spectra were measured with a double beam spectrometer (Cary 17 Varian).

All measurements were performed at room temperature.

3. Results

The optical density spectra, $OD = \log_{10}(I_0/I)$ [23], of the glasses are shown in Fig. 1, together with the location of the Ar laser lines. The inset shows the absorption bands of the chromate ion at 370 and at about 250 nm. The band centered at 650 nm is due to electronic transitions involving the ground state, ²A₄, and the excited state, ⁴T₂, of the Cr³⁺. Dips appear at 650 and 680 nm due to Fano anti-resonance effect, involving the forbidden levels, ²T₁ and ²E, respectively [24].

Fig. 2 shows the Raman spectra (90° scattering geometry) of the undoped and Cr_2O_3 doped glasses, using the 488.0 nm laser line. No data reduction [25] was made since, in the case of the doped glass, it is very difficult to determine the temperature in the optical path of the laser beam inside the sample.



Fig. 1. Absorption spectrum of the glass with 1.0 wt% Cr_2O_3 (thickness: 0.40 mm) in the range of the Ar laser lines. Inset: absorption spectrum of (a) the glass with about 0.1 wt% Cr_2O_3 (thickness: 0.25 mm), and (b) the glass with 1.0 wt% Cr_2O_3 (thickness: 2.88 mm).



Fig. 2. Raman spectra (90° scattering geometry) of the $2Na_2O$ · 1CaO·3SiO₂ glass samples: (a) undoped and (b) doped with 1.0 wt% Cr₂O₃ ($\lambda_i = 488$ nm, laser power: \approx 500 mW).

Moreover, the data reduction is an important procedure when the low frequency range of the spectrum of amorphous materials is analyzed [26].

The Raman spectrum (a), in Fig. 2, of the undoped glass presents intense bands at 625 and 978 cm^{-1} . The band at 625 cm^{-1} has an asymmetric shape and is attributed to superimposed symmetric and asymmetric bending vibration of O⁻-Si-O⁻ bonds [27]. The band at 978 cm^{-1} is a superposition



Fig. 3. Result of the subtraction of the undoped glass from the Cr_2O_3 doped glass Raman spectra of Fig. 2 after intensity normalization of the spectra with respect to the band at 625 cm⁻¹.

of symmetric stretching of SiO₄ tetrahedra with one, two and three non-bridging oxygens (NBO), and the 856 cm⁻¹ band is due to the symmetric stretching of the SiO₄ tetrahedra with four NBOs [27]. The very weak band at about 335 cm⁻¹ is related to the vibrations of the network modifier (Na⁺, Ca²⁺)– NBO bonds [28,29]. At low frequencies, the asymmetric band at 70 cm⁻¹ is the so called Raman– Stokes boson peak, related to the thermal population of phonons, a feature common in Raman spectra of amorphous materials [30,31]. The band in the vicinity of -70 cm⁻¹ is the Raman–anti-Stokes boson peak.

The Raman spectrum (b), in Fig. 2, is of the Cr_2O_3 doped glass. In addition to the bands observed in the undoped glass, an intense and narrow band appears at about 850 cm⁻¹, and a shoulder is located at about 890 cm⁻¹. A low intensity band appears at 365 cm⁻¹ with a shoulder at its high frequency side.



Fig. 4. Raman spectra (90° scattering geometry) of the 1.0 wt% Cr_2O_3 doped glass excited by the visible Ar laser lines. The spectra are normalized with respect to the intensity of the band at 625 cm⁻¹.

A better visualization of these bands is shown in Fig. 3, which is the result of the subtraction of both spectra in Fig. 2, normalized with respect to the band at 625 cm⁻¹, taken as an internal standard. The 'spectrum' which results from this subtraction is essentially similar to the spectrum of CrO_4^{2-} in aqueous solution [17].

The Raman spectra obtained with the 90° scattering geometry using the main visible Ar laser lines are presented in Fig. 4. The intensity of all the spectra are normalized with respect to the 625 cm⁻¹ band of the glass network spectrum. The intensity of the 850 cm⁻¹ band increases considerably when the exciting wavelength decreases, which is due to the pre-resonant Raman effect.

It must be emphasized that, with the classical 90° scattering geometry, there is an optical absorption of the scattered light inside the sample. The effect of the absorption in our analysis is partially removed by the normalization of the spectra with respect to the 625 cm^{-1} band which is expected to be subject to similar absorption effects. In order to clarify this point, we performed micro-Raman measurements on



Fig. 5. Micro-Raman spectra of the same sample as that of Fig. 4, also normalized with respect to the $625~{\rm cm}^{-1}$ band.



Fig. 6. Relative intensity of the $\tilde{\nu}_s = 850 \text{ cm}^{-1}$ Raman bands as a function of the exciting wavelength, λ_i . The open circles (O) are the experimental values taken from the spectra of Fig. 4, while the close circles (\bullet) were taken from Fig. 5. The dashed and dotted curves represent the adimensional factors F_B^2 (Eq. (2)) and F_A^2 (Eq. (1)), respectively, using $\tilde{\nu}_e = 27000 \text{ cm}^{-1}$, $\tilde{\nu}_f = 40000 \text{ cm}^{-1}$ and $\tilde{\nu}_i = \lambda_i^{-1}$. The solid curve is a fit to a visual guide of the micro-Raman results. Normalization has been made so that the intensity is equal to unity for $\lambda_i = 488.0 \text{ nm}$.

the surface of the sample, and the results are presented in Fig. 5.

Fig. 6 shows the dependence of the intensities of the 850 cm⁻¹ bands with the exciting wavelength taking $I_{\lambda_i}/I_{488} = 1$ for $\lambda_i = 488.0$ nm. The dashed curve is the representation of Eq. (2), using the absorption frequencies of the chromate ion: $\tilde{\nu}_e =$ 27 000 cm⁻¹ ($\lambda_e = 370$ nm) and $\tilde{\nu}_f = 40\,000$ cm⁻¹ ($\lambda_f = 250$ nm), while the dotted line represents Eq. (1). The 90° scattering geometry data are better fitted by the adimensional factor F_B^2 given by Eq. (2). In the case of the data obtained by a micro-Raman surface analysis, results of which are adjusted by the solid curve, the fit by Eq. (2) is less good. These results are discussed in the next section.

4. Discussion

The optical absorption bands at 370 and at 250 nm of the chromate ion (Fig. 1) are due to charge

transfer between the ligand (O⁻) and the metal ion (Cr^{6+}) [23], which produces a polarizability change of the molecular ion. While approaching the 370 nm band from higher wavelengths, there is an increase of the chromate ion polarizability. This increase produces the enhancement of the 850 cm⁻¹ Raman band intensity, and the pre-resonant Raman effect takes place.

The structure of silicate glasses, like other amorphous materials, is disordered for mid- and longrange. The interatomic bond lengths and bond angles have broad distributions, which is not the case for crystalline structures. These structural features are responsible for the broadening of the Raman bands of glasses by comparison with the narrower bands observed in crystalline materials with the same composition as the precursor glass [32,33].

The chromate ion Raman band at 850 cm⁻¹, seen in Figs. 2-5, is narrower than the bands of the glass matrix. Spectra similar to that shown in Fig. 3 were presented by Michel and Machiroux [17] and by Brawer and White [20] for chromate ions in aqueous solutions, and the band assignments are in accordance with the work of Stammreich et al. [15]. Such features lead us to conclude that the vibrational mode frequencies of the chromate ion are not influenced by the surrounding glass network. The absence of a vibrational coupling between the glass network and the chromate ions is an indication that these ions are isolated in the glass, and consequently there are no bonds such as $\equiv Cr - O - Si \equiv$ and \equiv Cr-O-Cr \equiv . This observation agrees with that made by Brawer and White [20].

Brown et al. [34] measured Raman and infrared spectra of solid Cr_2O_3 and assigned the chromiumoxygen stretching and bending modes on the basis of octahedrally coordinated Cr^{+3} ions. In their Raman spectrum, the band at 348 cm⁻¹ is attributed to the O-Cr-O bond deformation mode $\nu_5(F_{2g})$. This frequency is almost the same as for the CrO_4^{2-} symmetric bending mode, $\nu_2(E)$, indicated in Fig. 3. No other correspondence between the Cr_2O_3 Raman bands identified by Brown et al. and the $CrO_4 2$ – spectrum in Fig. 3 has been found. This may be explained by the lower concentration of Cr^{3+} than Cr^{6+} ions in the glass, and also by the low polarizability changes of the Cr^{3+} -O bond during vibrations.

Fig. 6 shows that Eq. (2) gives the best fit of the experimental data obtained with the 90° scattering geometry. However, the fit is less good for the micro-Raman data, obtained at the sample surface, in which case the absorption of the scattered light is negligible. It is important to emphasize that the theoretical models represented by Eqs. (1) and (2) do not take into account the damping associated to the optical absorption processes. Ovander [35] showed that the theoretical models which explain the resonant Raman scattering must be modified when the damping is large. In this case, the divergence of the scattering intensity is removed for $\tilde{\nu}_i = \tilde{\nu}_e$ (or $\tilde{\nu}_i =$ $\tilde{\nu}_{\rm f}$). Loudon [36] observed that, in the case of resonance Raman scattering, the Raman tensor is always finite due to the arrangement of the electronic energy levels in bands.

This feature can be qualitatively described by the addition of a damping term in the denominator of the scattering intensity expression, I_s [1,5,36,37]. The addition of a constant term in the denominator of Eqs. (1) and (2) would change the I_{λ_i}/I_{488} curve, shown in Fig. 6, in such a way that the new curve would pass below the displayed curve for $\lambda_i < 488$ nm and above this curve for $\lambda_i > 488$ nm. This result is in accordance with our micro-Raman experimental data.

5. Conclusions

The pre-resonant Raman effect observed for chromate ion in the $2Na_2O \cdot 1CaO \cdot 3SiO_2$ glass is qualitatively explained by the theory developed for two electronic transitions involved in the inelastic light scattering process; the dependence of the 850 cm⁻¹ band intensity with the exciting wavelength is better adjusted by the adimensional factor F_B^2 , given by Eq. (2). The theory must be improved by the introduction of a damping term in the equations considered in order to give a better adjustment of the experimental data.

Comparison made between Raman spectra of chromate ions in liquid solutions, in crystals and in glasses show no substantial differences with respect to frequencies, width and polarization of their bands. These observations reinforce early conclusions that there is no vibrational coupling between these ions and their vicinity, since the ions are dissolved in the glass network, coordinated by the modifier ions Na^+ and Ca^{2+} , to keep the electrical neutrality of the glass.

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References

- J. Behringer, in: Raman Spectroscopy Theory and Practice, ed. H.A. Szymanski (Plenum, New York, 1967) p. 168.
- [2] A.C. Albrecht and M.C. Hutley, J. Chem. Phys. 55 (1971) 4438.
- [3] M.C. Hutley and D.J. Jacobs, Chem. Phys. Lett. 3 (1969) 711.
- [4] J. Behringer and J. Brandmüller, Z. Elektrochem. 60 (1956) 643.
- [5] J. Behringer, Z. Elektrochem. 62 (1958) 906.
- [6] S.J. Doing and F.G. Prendergast, Appl. Spectrosc. 49 (1995) 247.
- [7] W. Kiefer and H.J. Bernstein, Appl. Spectrosc. 25 (1971) 500.
- [8] K. Ohwada, A. Takahashi and G. Fujisawa, Appl. Spectrosc. 49 (1995) 216.
- [9] T.E. Furtak and J. Reyes, Surf. Sci. 93 (1980) 351.
- [10] A. Campion, in: Vibrational Spectroscopy of Molecules on Surfaces, ed. J.T. Yates Jr. and T.E. Madey (Plenum, New York, 1987) p. 345.
- [11] J. Sapriel and B.D. Rouhani, Surf. Sci. Rep. 10 (1989) 189.
- [12] V.A. Gaisler, I.G. Neizvestnyi, M.P. Sinyukov and A.B. Talochkin, JETP Lett. 45 (1987) 441.
- [13] B. Champagnon, B. Andrianasold and E. Duval, J. Chem. Phys. 94 (1991) 5237.

- [14] C.S. Venkateswaran, Proc. Indian Acad. Sci. 7A (1938) 144.
- [15] H. Stammreich, D. Bassi and O. Sala, Spectrochim. Acta 12 (1958) 403.
- [16] A. Müller, E.J. Baran and P.J. Hendra, Spectrochim. Acta 25A (1969) 1654.
- [17] G. Michel and R. Machiroux, J. Raman Spectrosc. 14 (1983) 22.
- [18] W. Kiefer and H.J. Bernstein, in: Advances in Raman Spectroscopy (Proc. Third Int. Conf. on Raman Spectroscopy), ed. J.P. Mathieu (Heyden, London, 1973) p. 317.
- [19] L.W. Johnson and S.P. McGlynn, Chem. Phys. Lett. 7 (1970) 618.
- [20] S.A. Brawer and W.B. White, Mater. Res. Bull. 18 (1983) 959.
- [21] C. Nelson, T. Furukawa and W.B. White, Mater. Res. Bull. 18 (1983) 959.
- [22] P. Nath and R.W. Douglas, Phys. Chem. Glasses 6 (1965) 197.
- [23] G.H. Siegel Jr., in: Treatise on Materials Science and Technology, ed. H. Herman, Vol. 12 (Academic Press, New York, 1977) p. 5.
- [24] A. Lempicki, L. Andrews, S.O. Nettel, B.C. McCollum and E.I. Solomon, Phys. Rev. Lett. 44 (1980) 1234.
- [25] R.M. Almeida, J. Non-Cryst. Solids 106 (1988) 347.
- [26] V.K. Malinovskii, V.N. Novikov and A.P. Sokolov, Sov. J. Glass Phys. Chem. 15 (1988) 163.
- [27] E.C. Ziemath and M.A. Aegerter, J. Mater. Res. 9 (1994) 216.
- [28] Y. Tsunawaki, N. Iwamoto, T. Hattori and A. Mitsuishi, J. Non-Cryst. Solids 44 (1981) 369.
- [29] Gan Fuxi, Huang Guosong and Chen Shizheng, J. Non-Cryst. Solids 52 (1982) 203.
- [30] M. Hass, J. Phys. Chem. Solids 31 (1970) 415.
- [31] V.K. Malinovsky and A.P. Sokolov, Solid State Commun. 57 (1986) 757.
- [32] S.K. Sharma, J.F. Mammone and M.F. Nicol, Nature 292 (1981) 140.
- [33] T. Furukawa and W.B. White, J. Mater. Sci. 16 (1981) 2689.
- [34] D.A. Brown, D. Cunningham and W.K. Glass, Spectrochim. Acta 24A (1968) 965.
- [35] L.N. Ovander, Sov. Phys. Solid State 4 (1962) 1081.
- [36] R. Loudon, J. Phys. (Paris) 26 (1965) 677.
- [37] G.W. Chantry, in: The Raman Effect, ed. A. Anderson, Vol. 1 (Dekker, New York, 1971) p. 49.